#### Species Tree Inference

2014 Bodega Bay Applied Phylogenetics Workshop

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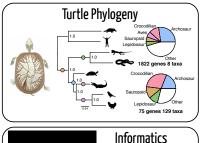
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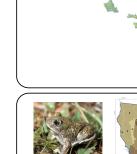
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#### **Overview**

- Think a bit about phylogenetic reconstruction
- Do our simplifications cause problems?
- A few cases where they might, and how we might deal with those issues when they arise.

#### Research interests







Hawaiian Radiations

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#### Sources of gene tree variation

• Incomplete coalescence



Horizontal transfer

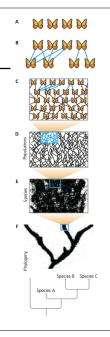


• Gene duplication



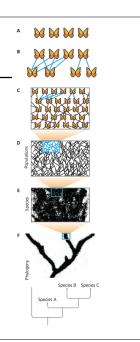
#### Anatomy of a tree

- What are phylogenetic lineages?
  - Each species lineage implicitly contains populations of reproducing populations
  - Phylogenies among species are simplifying this process



#### Anatomy of a tree

- Let's say we want to infer a phylogeny of these 3 butterfly species
  - We collect data for an individual from each species and infer a phylogeny

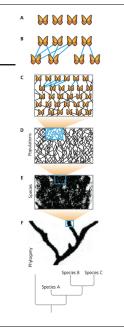


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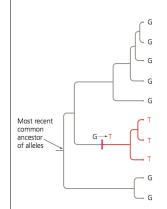
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#### Anatomy of a tree

- Let's say we want to infer a phylogeny of these 3 butterfly species
  - We collect data for an individual from each species and infer a phylogeny
  - Implicitly, we're saying that the evolutionary relationships among those three <u>individuals</u> match the evolutionary relationships among the three <u>species</u>
  - Can this cause problems?



#### **Molecular Phylogenetics**



• This is a simplification

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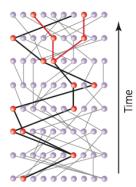
- The G->T substitution is a population genetic process
- i.e., a single mutation occurred in one individual in an ancestral population. It then increased in frequency until it became fixed in the whole species.

#### Molecular Phylogenetics

- We need to connect our simplified phylogenies of species to trees of individuals
  - We can build a model for this
  - Will start with a case involving only a single species
    - The coalescent
  - Then extend to multiple species
    - The multispecies coalescent

#### The coalescent model

- Imagine a single species made up of N diploid individuals (2n total alleles)
  - Let's think about the relationships between all of those alleles
    - Here alleles simply refer to physical copies of a particular locus, not distinct forms of that locus



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#### The coalescent model

• How many generations ago did these alleles last share a common ancestor?











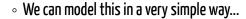




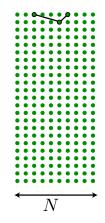
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#### The coalescent model

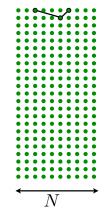


• The probability of 2 lineages coalescing is



 $\circ$  The probability of 2 lineages coalescing is the probability of them choosing the same ancestor:  $\underbrace{1}_{-}$ 

#### The coalescent model



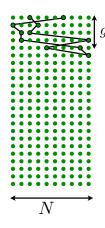
 $\circ$  The probability of 2 lineages coalescing is the probability of them choosing the same ancestor:  $\frac{1}{N}$ 

 $\,{}_{\circ}\,$  Because of this, the expected time until coalescence is simply  $\,N\,$ 

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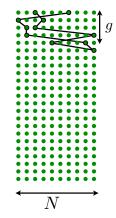
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#### The coalescent model



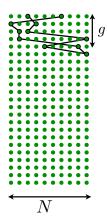
 Probability that coalescence occurs g+1 generations back:

#### The coalescent model



- Probability that coalescence occurs g+1 generations back:
  - Probability of no coalescence for g generations

$$(1 - \frac{1}{N}) \times (1 - \frac{1}{N}) \dots = (1 - \frac{1}{N})^g$$

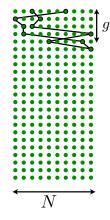


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• followed by coalescence

#### The coalescent model



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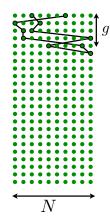
 $\circ$  followed by coalescence  $\frac{1}{N}$ 

$$=\frac{1}{N}(1-\frac{1}{N})^g$$

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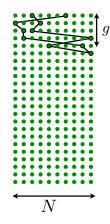
#### The coalescent model



$$=\frac{1}{N}(1-\frac{1}{N})^g$$

- This is the geometric distribution
  - Describes the time of the first success for independent trials with probability of success p and probability of failure (1-p)
  - ∘ Rate = p or 1/N
  - ∘ Mean = 1/p or N

#### The coalescent model



 Probability of coalescence event (or success rate) among n sampled lineages is



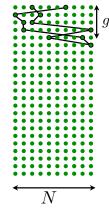
 Probability of coalescence event (or success rate) among n sampled lineages is

$$\frac{\binom{n}{2}}{N}$$

 n choose 2 accounts for the variety of ways that coalescence can occur

$$\frac{n!}{2!(n-2)!}$$

The coalescent model



 Probability of coalescence event (or success rate) among n sampled lineages is

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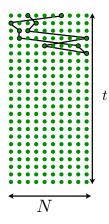
$$\frac{n!}{2!(n-2)!}$$

• Probability of event g+1 generations back:

$$\frac{\binom{n}{2}}{N}(1-\frac{\binom{n}{2}}{N})^g$$

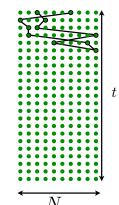
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The coalescent model



Geometric distribution is a discrete time distribution

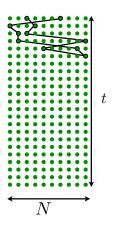
The coalescent model



- Geometric distribution is a discrete time distribution
- Continuous time version is the exponential distribution

$$\lambda e^{-\lambda t}$$

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- Geometric distribution is a discrete time distribution
- Continuous time version is the exponential distribution

$$\lambda e^{-\lambda t}$$

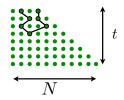
 As N goes to infinity, the coalescent process converges to a continuous time markov process with instantaneous rate of coalescence:

$$\lambda = \frac{\binom{n}{2}}{N}$$

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#### The coalescent model

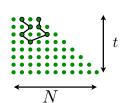
We've been assuming constant population size



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#### The coalescent model

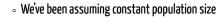
• We've been assuming constant population size

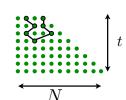


 Instead of N, we can specify a function that describes a changing population size through time

$$N \longrightarrow N(t)$$

#### The coalescent model





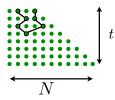
 Instead of N, we can specify a function that describes a changing population size through time

$$N \longrightarrow N(t)$$

 Our instantaneous rate of coalescence is a function of N, so we need to integrate the rate of coalescence across the function for N

$$\frac{\binom{n}{2}}{N}e^{-\frac{\binom{n}{2}}{N}t} \longrightarrow \frac{\binom{n}{2}}{N(t)}\exp\left(-\int_0^t \frac{\binom{n}{2}}{N(t)}dt\right)$$

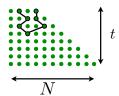
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 We have a nice function to calculate the probability of one coalescent event occurring at time t, given a demographic function of t:

$$\uparrow t \quad P(t) = \frac{\binom{n}{2}}{N(t)} \exp\left(-\int_0^t \frac{\binom{n}{2}}{N(t)} dt\right)$$

#### The coalescent model



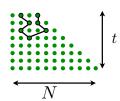
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• What is the probability of <u>all</u> coalescent events observed in a sample?

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#### The coalescent model

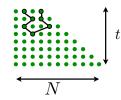


 We have a nice function to calculate the probability of one coalescent event occurring at time t, given a demographic function of t:

- What is the probability of <u>all</u> coalescent events observed in a sample?
  - $\circ$  Given a demographic function and a list of coalescence times  $\ \, {\bf L}=(0,t_n,t_{n-1},\ldots)$

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#### The coalescent model



 We have a nice function to calculate the probability of one coalescent event occurring at time t, given a demographic function of t:

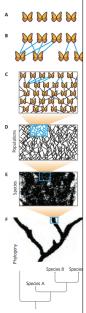
$$\int_{t} P(t) = \frac{\binom{n}{2}}{N(t)} \exp\left(-\int_{0}^{t} \frac{\binom{n}{2}}{N(t)} dt\right)$$

- What is the probability of <u>all</u> coalescent events observed in a sample?
  - $\circ$  Given a demographic function and a list of coalescence times  $\ L=(0,t_n,t_{n-1},\ldots)$
  - 。Each event is independent, so take the product

$$\mathrm{P}(L|N(t)) = \prod_{i=2}^{n} \frac{\binom{n}{2}}{N(t)} \mathrm{exp}\left(-\int_{0}^{t} \frac{\binom{n}{2}}{N(t)} dt\right)$$

 Starting with first principles, we can derive a model that describes the probability of coalescence histories within a lineage The coalescent model

- Starting with first principles, we can derive a model that describes the probability of coalescence histories within a lineage
- Connects our simplified idea of a phylogenetic lineage back to the underlying individual sampling



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#### The coalescent model

- Starting with first principles, we can derive a model that describes the probability of coalescence histories within a lineage
- Connects our simplified idea of a phylogenetic lineage back to the underlying individual sampling
- We end up with an equation that allows us to calculate the likelihood of an observed set of coalescence times within a lineage

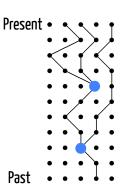
 $P(L|N(t)) = \prod_{i=2}^{n} \frac{\binom{n}{2}}{N(t)} \exp\left(-\int_{0}^{t} \frac{\binom{n}{2}}{N(t)} dt\right)$ 

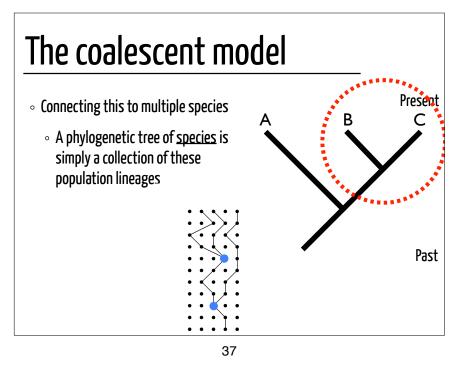
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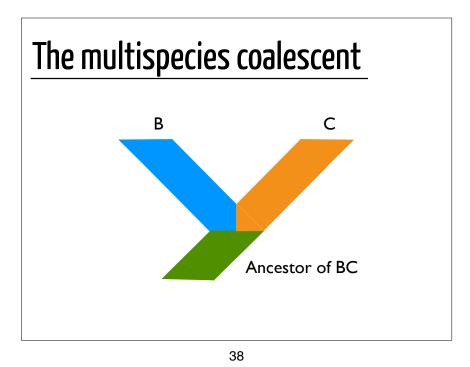
#### The coalescent model

#### THE IMPORTANT THING TO REMEMBER:

- Probability of coalescence within a population depends on:
  - Population size
  - Number of generations







The multispecies coalescent

A

B

C

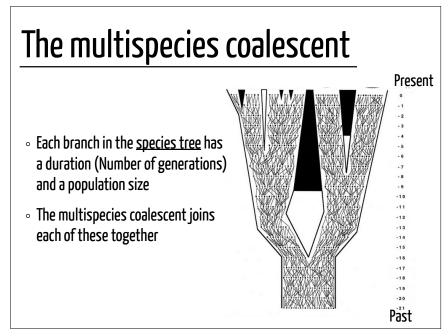
Containing tree

= species tree

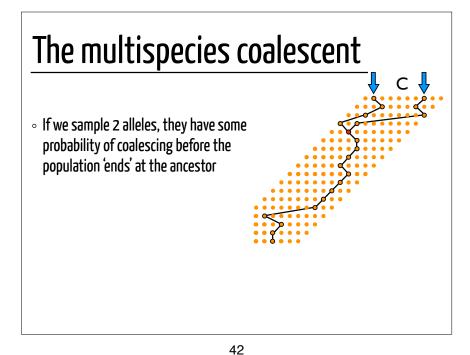
Contained tree

= gene tree

Maddison 1997

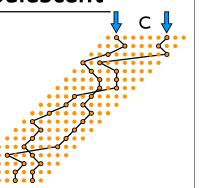


# The multispecies coalescent B C Ancestor of BC



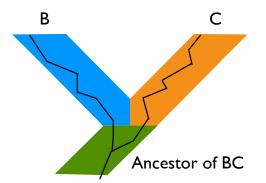
The multispecies coalescent

- If we sample 2 alleles, they have some probability of coalescing before the population 'ends' at the ancestor
- Which means they also have some probability of <u>not</u> coalescing
- Depends on the population size and the number of generations



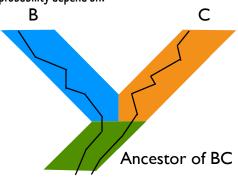
The multispecies coalescent

 Likewise, if we sample one allele from each of two <u>different</u> species, there is some probability that the two alleles will coalesce in the ancestor



#### The multispecies coalescent

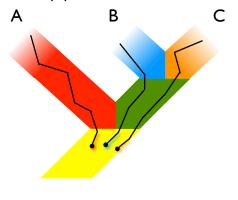
- But there is also some probability that they will not.
  - This is called incomplete coalescence
- What does the probability depend on?



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#### The multispecies coalescent

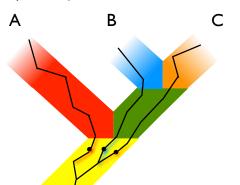
 If they don't coalesce within the ancestor, they move down into the next ancestral population

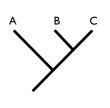


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#### The multispecies coalescent

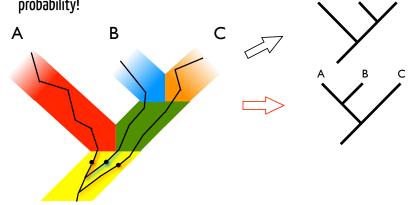
 Now they can coalesce in 3 different ways with equal probability!





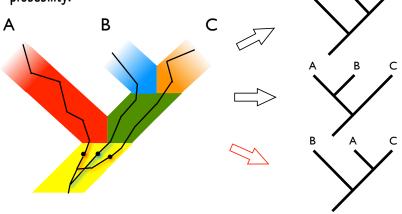
#### The multispecies coalescent

 Now they can coalesce in 3 different ways with equal probability!



#### The multispecies coalescent

 Now they can coalesce in 3 different ways with equal probability!



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#### The multispecies coalescent

- Only 1 of the 3 matches the actual species phylogeny
  - So if there is an incomplete coalescence event in the alleles that we sampled, we have a 2/3rds chance of getting the wrong tree
- How do we determine the probability of incomplete coalescence?

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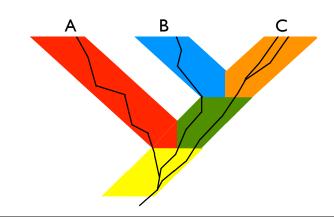
#### The multispecies coalescent

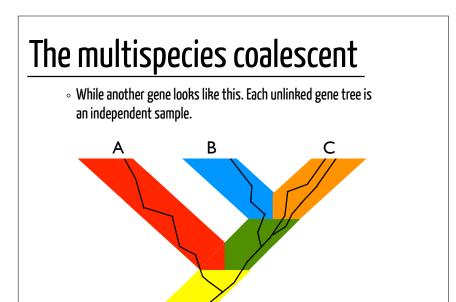
- The probability depends on the coalescent process that occurs within each lineage
  - We can break up the tree into its component parts
  - Each part has an 'input' and an 'output' number of lineages
    - Inherits the input from what happens above it
    - Output depends on the population size and the duration of the branch

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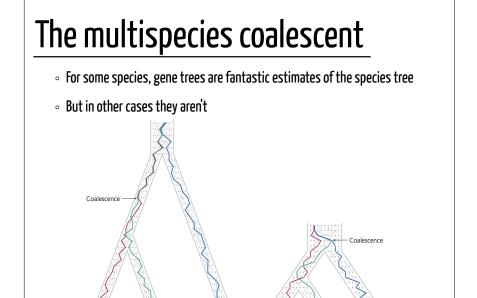
#### The multispecies coalescent

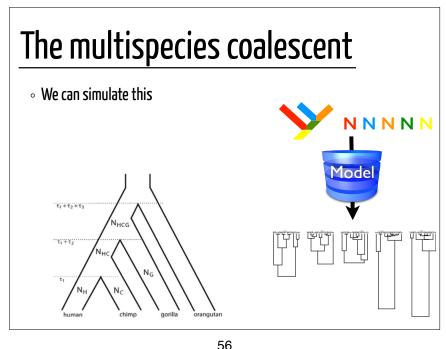
• Gene 1 might look like this





The multispecies coalescent
So does our phylogenetic sampling cause problems?
I.e., does our tree of individuals match our tree of species?
Answer: Not necessarily, it depends on the population sizes and durations





#### **Empirical Example**

OPEN & ACCESS Freely available online

PLOS GENETICS

Widespread Discordance of Gene Trees with Species Tree in *Drosophila*: Evidence for Incomplete Lineage Sorting

Daniel A. Pollard<sup>1</sup>, Venky N. Iyer<sup>2</sup>, Alan M. Moses<sup>1</sup>, Michael B. Eisen<sup>1,2,3,4\*</sup>

- Genomic data for each of:
  - 。 D. ananassae outgroup
  - D. melanogaster
  - D. erecta
  - D. yakuba

Pollard et al. 2006

### **Empirical Example**

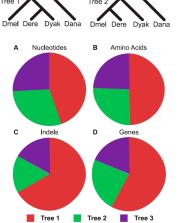




Pollard et al. 2006

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#### **Empirical Example**



Tree 3

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Nucleotide substitutions (in 9405 genes): Tree1-170,002, Tree 2-112,278, Tree 3-98,117.

Gene trees (under ML): Tree 1- 5,381, Tree 2- 2,188, Tree 3-1,746

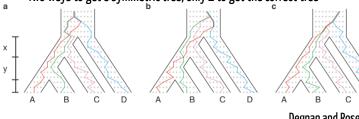
Conclude: Tree 1 ((erecta,yakuba), melano) wins, but lineage sorting is a huge problem.

Pollard et al. 2006

#### Anomolous gene trees

- There are cases where the wrong tree is more likely to be inferred than the correct tree
- 4 taxon asymmetric tree
  - If branches x and y are short -> lineages join randomly

• Two ways to get a symmetric tree, only 1 to get the correct tree



Degnan and Rosenberg 2006

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#### **Empirical Example**

- Human, Chimp, Gorilla
- Look at distribution of genome trees across the entire genome

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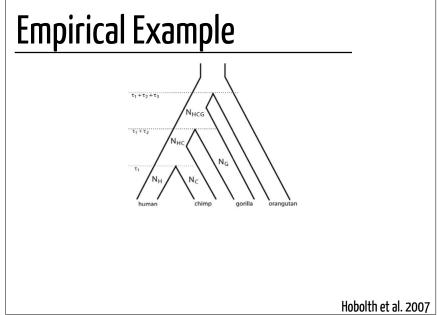
PLOS GENETICS

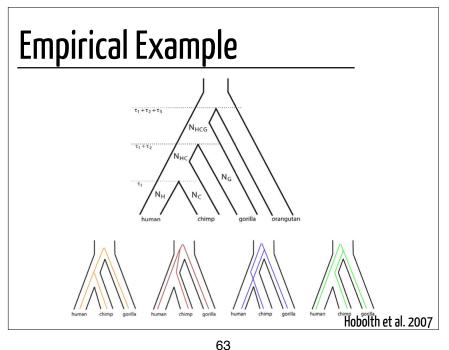
Genomic Relationships and Speciation Times of Human, Chimpanzee, and Gorilla Inferred from a Coalescent Hidden Markov Model

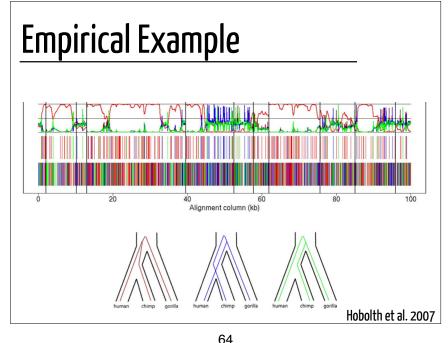
Asger Hobolth<sup>1\*</sup>, Ole F. Christensen<sup>2</sup>, Thomas Mailund<sup>2,3</sup>, Mikkel H. Schierup<sup>2</sup>

1 Bioinformatics Research Center, North Carolina State University, Raleigh, North Carolina, United States of America, 2 Bioinformatics Research Center, University of Aarhus, Aarhus, Denmark, 3 Department of Statistics, University of Oxford, Oxford, United Kingdom

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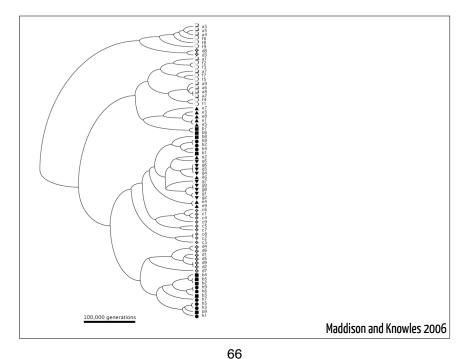


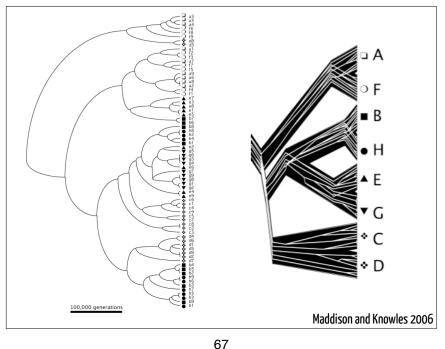




#### Minimize Deep Coalescence

 given a set of gene trees, find the species tree that minimizes the implied number of deep coalescences (Maddison 1997, Maddison and Knowles 2006)





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#### Minimize Deep Coalescence

- simple and intuitive
- but ignores important information (branch lengths), no measure of support
- software packages
  - mesquite
  - ∘ deep
  - Phylonet
- Doesn't explicitly model the coalescent process, places all probably on single histories

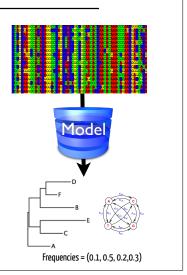
#### Multispecies coalescent inference

- Perhaps a better solution:
  - We have this nice model, we can use statistical inference to infer species trees from gene trees and/or alignments

Statistical inference

• What we've been doing:

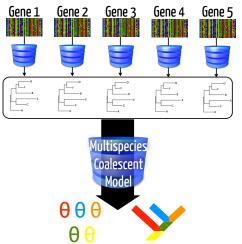
 Inference under the MC, in the most general case, involves adding another level to this model.

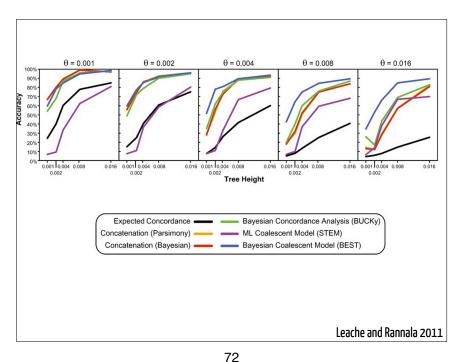


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## The multispecies coalescent Gene 1 Gene 2 Gene 3 Gene 4 Gene 5





#### \*BEAST Model

$$P(S|D) = \frac{\prod_{i=1}^{n} P(d_i|g_i)P(g_i|S)P(S)}{P(D)}$$

• 4 components:

Heled and Drummond 2010

#### \*BEAST Model

$$P(S|D) = \frac{\prod_{i=1}^{n} P(d_i|g_i)P(g_i|S)P(S)}{P(D)}$$

• 4 components:

 $\circ P(d_i|g_i)$ - standard likelihood for alignment and gene tree i

Heled and Drummond 2010

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$$P(S|D) = \frac{\prod_{i=1}^{n} P(d_i|g_i)P(g_i|S)P(S)}{P(D)}$$

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 $_{\circ}P(g_{i}|S)$ - coalescent likelihood of gene trees

Heled and Drummond 2010

#### \*BEAST Model

$$P(S|D) = \frac{\prod_{i=1}^{n} P(d_i|g_i)P(g_i|S)P(S)}{P(D)}$$

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 $\circ P(d_i|g_i)$ - standard likelihood for alignment and gene tree i

 ${}_{\circ}P(g_i|S)$ - coalescent likelihood of gene trees

 $\circ \ P(S)$  - uniform topology P(D) - normalizing constant

- birth-death or Yule branching

- gamma pop sizes with hyperprior

Heled and Drummond 2010

#### \*BEAST

$$P(g_i|S)$$

- Likelihood of gene trees given the species tree
- We have an equation to calculate the likelihood of coalescent histories within a lineage

$$P(L|N(t)) = \prod_{i=2}^{n} \frac{\binom{n}{2}}{N(t)} \exp\left(-\int_{0}^{t} \frac{\binom{n}{2}}{N(t)} dt\right)$$

• How might we extend this to a whole tree?

Heled and Drummond 2010

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#### \*BEAST

 Answer: take the product of the coalescent likelihood along each branch

$$P(g|S) = \prod_{b \in S} P(L_b(g)|N_b(t))$$

Heled and Drummond 2010

#### \*BEAST

 Answer: take the product of the coalescent likelihood along each branch

$$=\prod_{i=2}^{n}\frac{\binom{n}{2}}{N(t)}\exp\left(-\int_{0}^{t}\frac{\binom{n}{2}}{N(t)}dt\right)\times$$

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Heled and Drummond 2010

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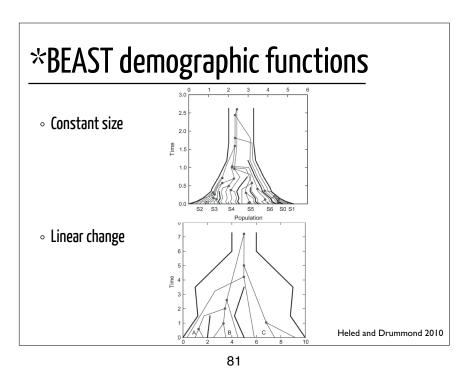
#### \*BEAST

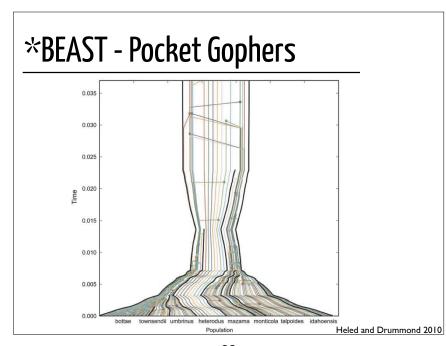
$$P(S|D) = \frac{\prod_{i=1}^{n} P(d_i|g_i)P(g_i|S)P(S)}{P(D)}$$

- Assumptions and limitations:
  - lineage sorting only source of incongruence
  - no gene flow following speciation
  - Implements a couple of demographic functions

Heled and Drummond 2010

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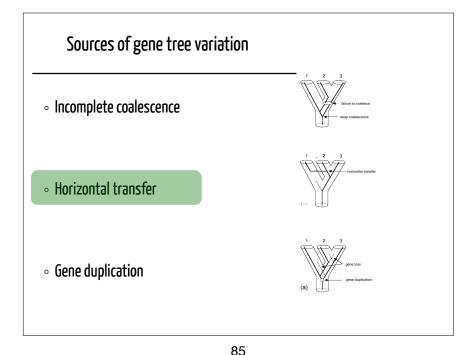




```
**BEAST

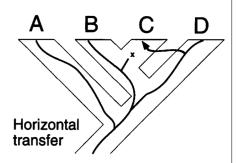
(1— The list of taxa to be analysed (can also include dates/ages).

(1— ntax=26
(taxa i | d= taxa")
(taxa i | d= tax
```



Horizontal gene transfer

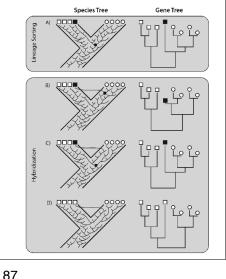
- Caused by hybridization or transfer via vectors
- Leads to a network like species history
- Can occur in conjunction with incomplete coalescence



Maddison 1997

Horizontal gene transfer

- Work on this is also emerging
- One basic idea is to use the distribution of branching times to detect shallow branching events that are unlikely under the coalescent



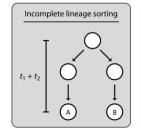
Joly et al. 2012

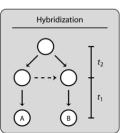
Horizontal gene transfer

 One approach: uses a technique called posterior predictive simulation to assess the probability of observing "young" nodes under the multispecies coalescent by itself

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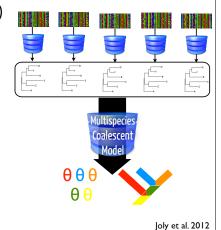




Joly et al. 2012

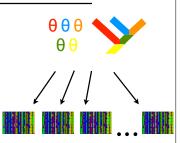
#### Horizontal gene transfer

- Steps for posterior predictive simulation:
  - perform species tree analyses (\*BEAST)



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  - Sample species trees, branch lengths, and population sizes from the posterior distribution
  - Use these samples to simulate sequences

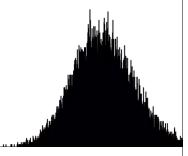


Joly et al. 2012

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#### Horizontal gene transfer

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  - Find the minimum pairwise distance between simulated sequences for your species of interest



Posterior predictive distribution of minimum pairwise divergences

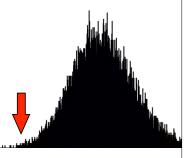
Joly et al. 2012

#### Horizontal gene transfer

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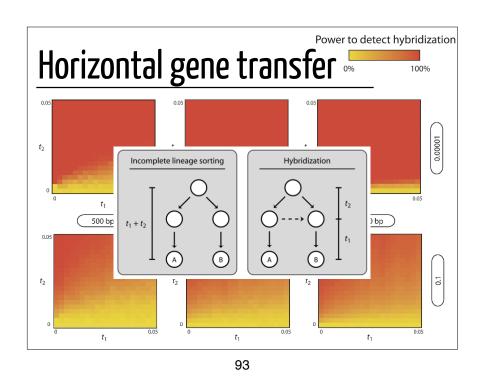
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  - Find the minimum pairwise distance between simulated sequences for your species of interest
  - Compare the minimum observed pairwise difference to construct p-value

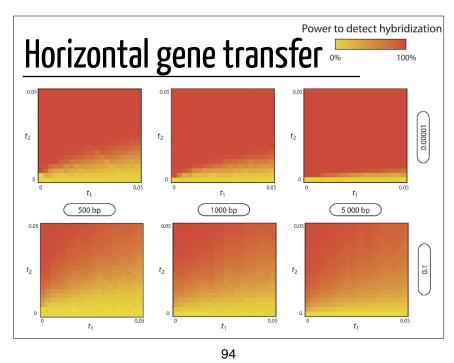
 $p = P(minDist(AB) < mindDist(AB)^{sim})$ 

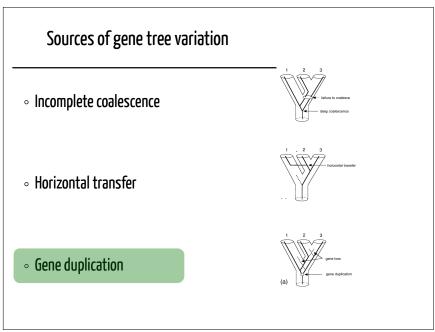


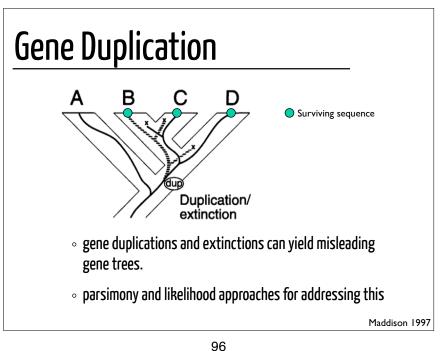
Posterior predictive distribution of minimum pairwise divergences

Joly et al. 2012









#### **Gene Duplication**

- One solution: Just avoid the problem altogether
  - This may often be the best option

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#### **Gene Duplication**

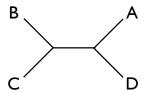
- One solution: Just avoid the problem altogether
  - This may often be the best option
- For well characterized genomes, focus on known single copy genes
- More problematic with large genome scale datasets
  - Need to be careful about automated homology assignment

#### Gene Tree Parsimony

- input a collection of rooted gene trees, find the species tree that minimizes the reconciliation cost
  - reconciliation cost is number of duplications, or duplications and losses, summed across gene trees

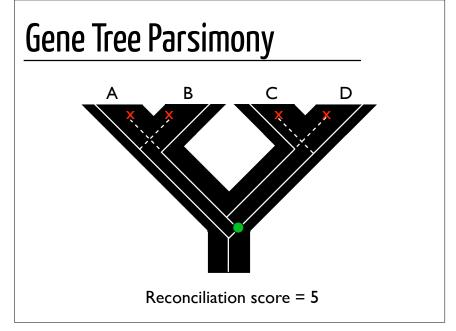
#### Gene Tree Parsimony

• example gene tree:



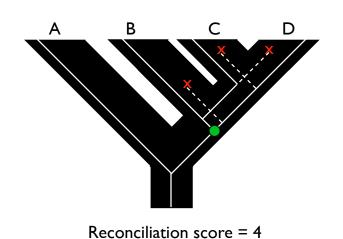
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• calculate reconciliation costs for species trees

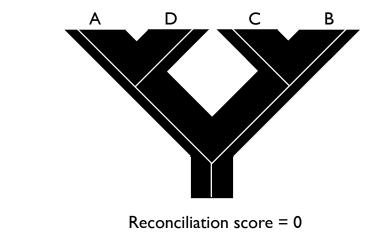


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#### Gene Tree Parsimony

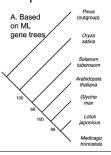


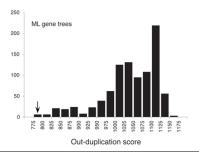
## Gene Tree Parsimony



#### **Empirical Example**

- Sanderson and McMahon 2007
  - GTP analysis of 576 gene trees for 6 angiosperm species (plus outgroup)
  - known species tree recovered successfully despite massive gene duplication





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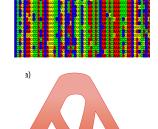
#### Gene Tree Parsimony

- small trees Gtp (Sanderson and McMahon 2007)
- ∘ large trees DupTree (Wehe et al 2008)

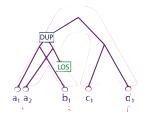
106

#### Statistical Approaches

 Likelihood methods for inferring gene trees and duplication and loss history given a species tree have existed for some time

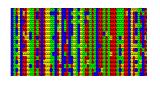


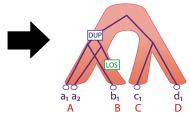




#### Statistical Approaches

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- Until recently, no methods available to do the joint inference





Boussau et al. 2013

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$$L(T, S, N|A) = \prod_{i \in \mathcal{G}} L(S, N|T_i) L(T_i|A_i)$$

Boussau et al. 2013

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Boussau et al. 2013

#### Statistical Approaches

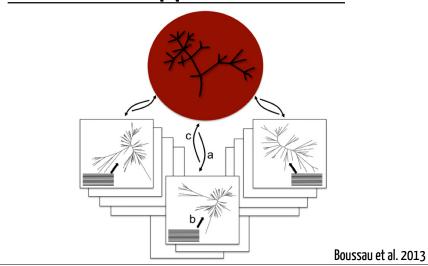
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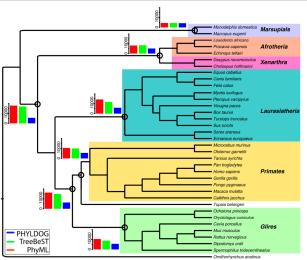
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#### **Statistical Approaches**



### **Statistical Approaches**



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Sources of gene tree variation

• Incomplete coalescence



Horizontal transfer



• Gene duplication



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#### Sources of gene tree variation

The inference of gene trees with species trees

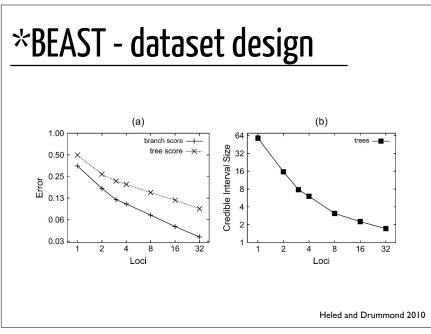
GERGELY J. SZÖLLŐSI<sup>1</sup>, ERIC TANNIER<sup>2,3,4</sup>, VINCENT DAUBIN<sup>2,3</sup>, BASTIEN BOUSSAU<sup>2,3</sup>

• Data needs are substantial

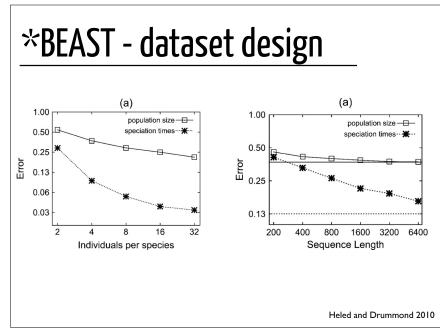
#### Wrapping up

- Some thoughts:
  - There are several options here, you should carefully choose a model based on biological knowledge
  - Need for more simulation studies
    - Sensitivities to priors and demographic functions

arXiv: 1311.0651v1 115



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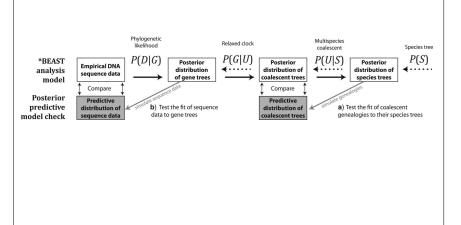


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#### **Difficulties**

- Often making some strong assumptions:
  - changes or constancy of population size
  - species membership and assignments
  - sources of gene tree variation
  - Not always well known how robust it is to deviations from the correct model

#### **Coalescent model plausibility**



Reid et al. 2013

## 

## the end