### Species Tree Inference

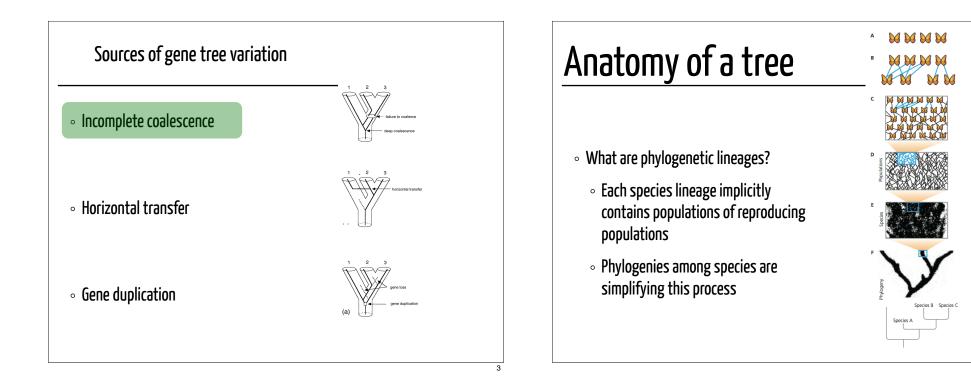
2013 Bodega Bay Applied Phylogenetics Workshop

Bob Thomson thomsonr@hawaii.edu thomsonlab.org



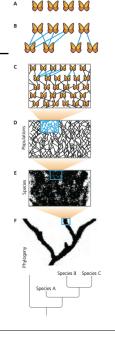
### **Overview**

- Think a bit about phylogenetic reconstruction
- Do our simplifications cause problems?
- A few cases where they might, and how we might deal with those issues when they arise.



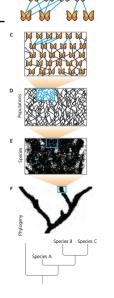
# Anatomy of a tree

- Let's say we want to infer a phylogeny of these 3 butterfly species
  - We collect data for an individual from each species and infer a phylogeny

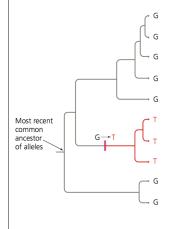


## Anatomy of a tree

- Let's say we want to infer a phylogeny of these 3 butterfly species
  - We collect data for an individual from each species and infer a phylogeny
  - Implicitly, we're saying that the evolutionary relationships among those three <u>individuals</u> match the evolutionary relationships among the three <u>species</u>
  - Can this cause problems?



### Molecular Phylogenetics



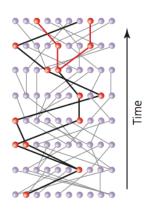
- This is a simplification
  - The G->T substitution is a population genetic process
  - i.e., a single mutation occurred in one individual in an ancestral population. It then increased in frequency until it became fixed in the whole species.

### Molecular Phylogenetics

- We need to connect our simplified phylogenies of species to trees of individuals
  - $\circ\,$  We can build a model for this
  - $\,\circ\,$  Will  $\,$  start with a case involving only a single species  $\,$ 
    - <u>The coalescent</u>
  - $\circ\,$  Then extend to multiple species
    - The multispecies coalescent

### The coalescent model

- Imagine a single species made up of N diploid individuals (2n total alleles)
  - Let's think about the relationships between all of those alleles
    - Here alleles simply refer to physical copies of a particular locus, not distinct forms of that locus



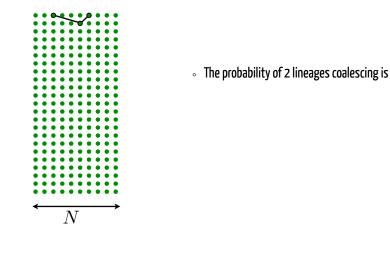
### The coalescent model

• How many generations ago did these alleles last share a common ancestor?



• We can model this in a very simple way...

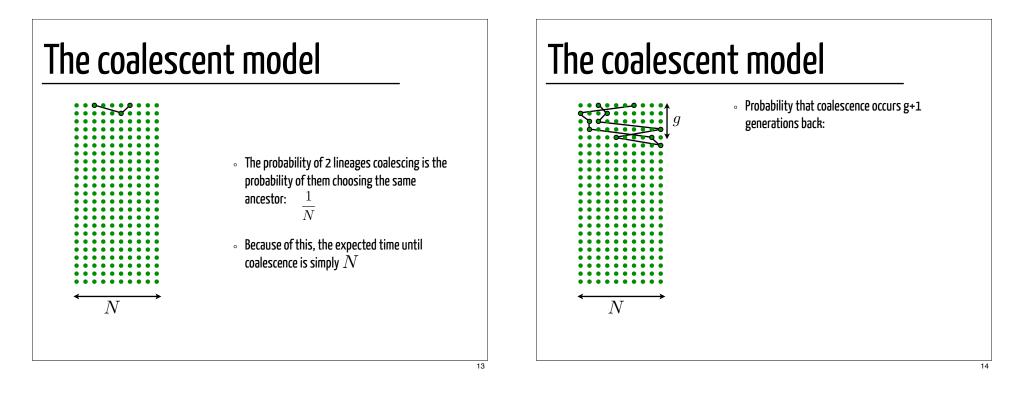
### The coalescent model

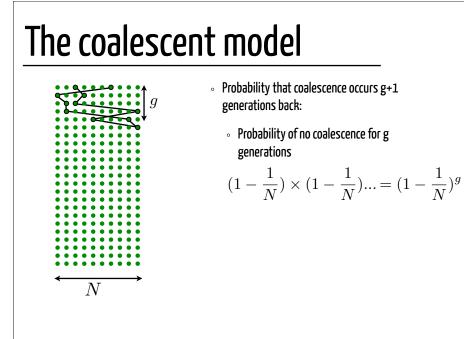


### The coalescent model

N

 $\circ~$  The probability of 2 lineages coalescing is the probability of them choosing the same ancestor:  $\frac{1}{N}$ 





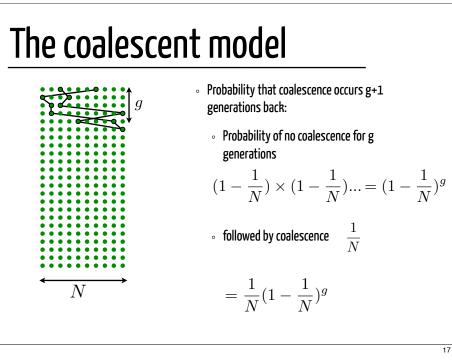
## The coalescent model

N

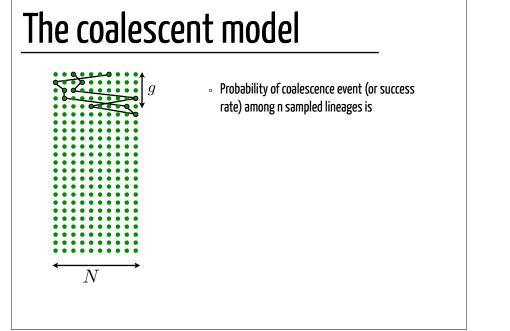
- Probability that coalescence occurs g+1 generations back:
  - Probability of no coalescence for g generations

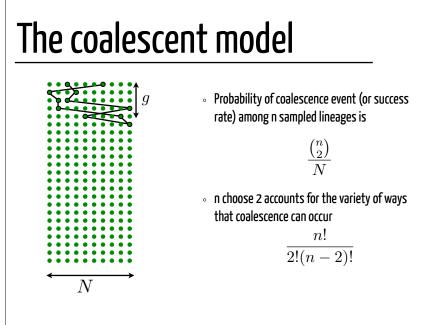
$$(1 - \frac{1}{N}) \times (1 - \frac{1}{N}) \dots = (1 - \frac{1}{N})^{\frac{1}{2}}$$

$$\circ$$
 followed by coalescence  $\frac{1}{N}$ 

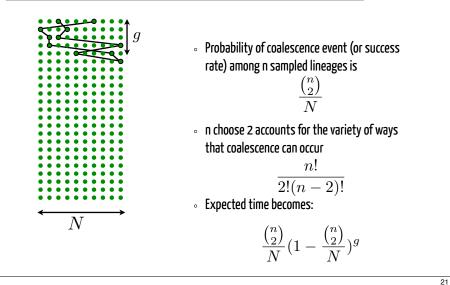


# The coalescent modelg $= \frac{1}{N}(1-\frac{1}{N})^g$ g $= \frac{1}{N}(1-\frac{1}{N})^g$ $\cdot$ This is the geometric distribution $\cdot$ Describes the time of the first success for independent trials with probability of success p and probability of failure (1-p) $\cdot$ Rate = p or 1/N $\cdot$ Mean = 1/p or N





### The coalescent model



# The coalescent model • Geometric distribution is a discrete time distribution

<section-header>
 Continuous time version is the exponential distribution
 t
 Continuous time version is the exponential distribution
 Continuous time version is the exponential distribution

The coalescent model

N

N

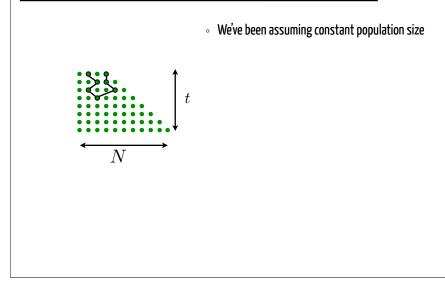
- Geometric distribution is a discrete time distribution
- Continuous time version is the exponential distribution

$$\lambda e^{-\lambda t}$$

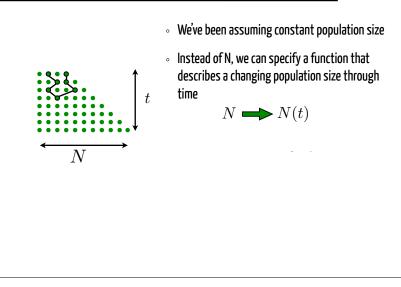
• As N goes to infinity, the coalescent process converges to a continuous time markov process with instantaneous rate of coalescence:

 $\lambda = \frac{\binom{n}{2}}{N}$ 

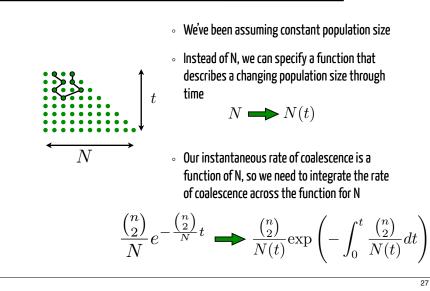
### The coalescent model



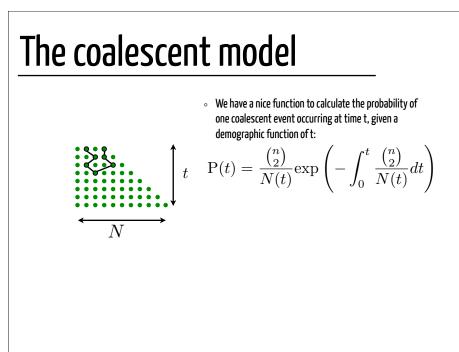
### The coalescent model

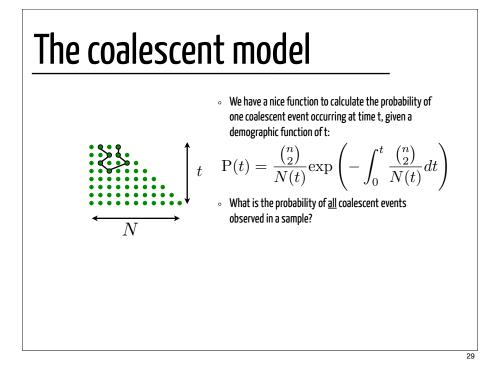


### The coalescent model



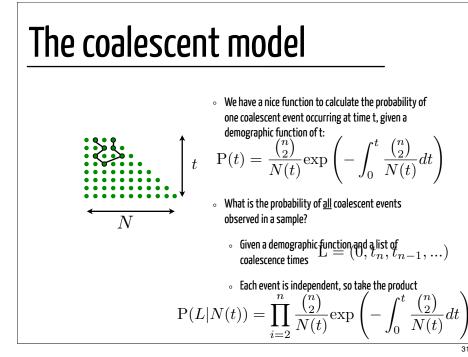
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# The coalescent model• We have a nice function to calculate the probability of<br/>one coalescent event occurring at time t, given a<br/>demographic function of t:t $P(t) = \frac{\binom{n}{2}}{N(t)} \exp\left(-\int_{0}^{t} \frac{\binom{n}{2}}{N(t)} dt\right)$

- What is the probability of <u>all</u> coalescent events observed in a sample?
  - $\circ~$  Given a demographic function and a list of coalescence times ~  $\mathbf{L}=(0,t_n,t_{n-1},\ldots)$

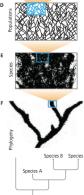


### The coalescent model

 Starting with first principles, we can derive a model that describes the probability of coalescence histories within a lineage

### The coalescent model

- Starting with first principles, we can derive a model that describes the probability of coalescence histories within a lineage
- Connects our simplified idea of a phylogenetic lineage back to the underlying population genetics



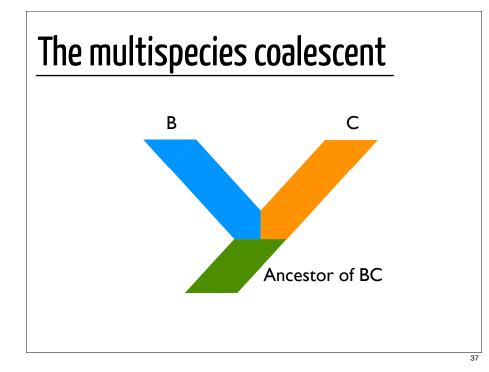
33

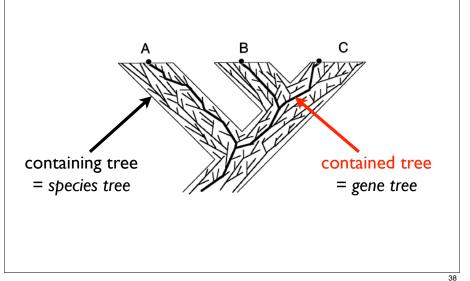
### The coalescent model

- Starting with first principles, we can derive a model that describes the probability of coalescence histories within a lineage
- Connects our simplified idea of a phylogenetic lineage back to the underlying population genetics
- We end up with an equation that allows us to calculate the likelihood of an observed set of coalescence times within a lineage

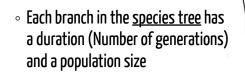
$$\mathsf{P}(L|N(t)) = \prod_{i=2}^{n} \frac{\binom{n}{2}}{N(t)} \exp\left(-\int_{0}^{t} \frac{\binom{n}{2}}{N(t)} dt\right)$$

# Connecting this to multiple species A phylogenetic tree of <u>species</u> is simply a collection of these population lineages

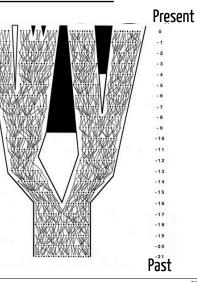


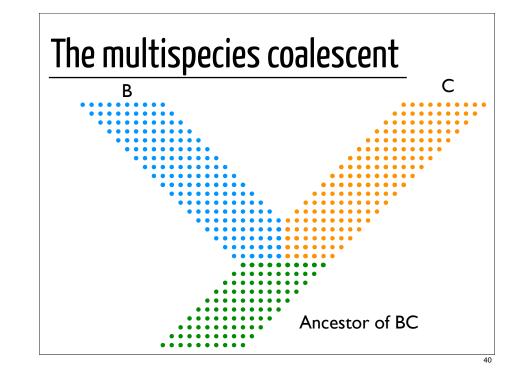


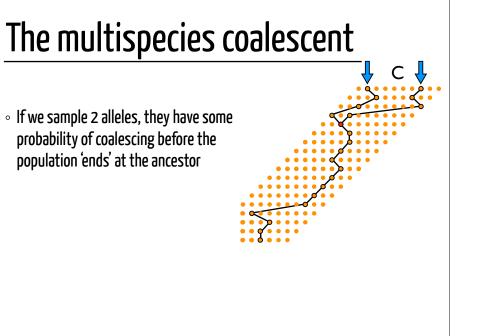
### The multispecies coalescent

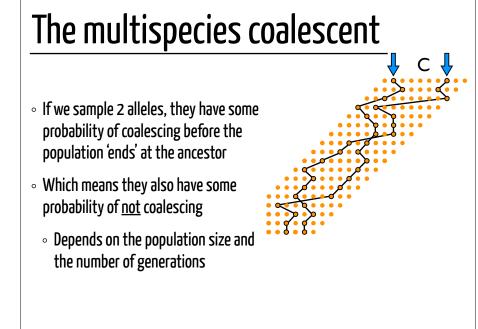


• The multispecies coalescent joins each of these together

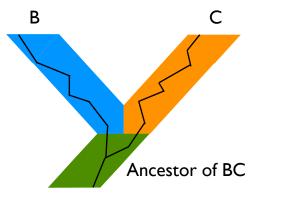






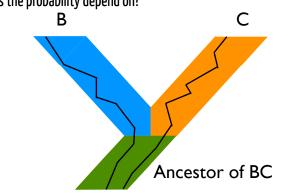


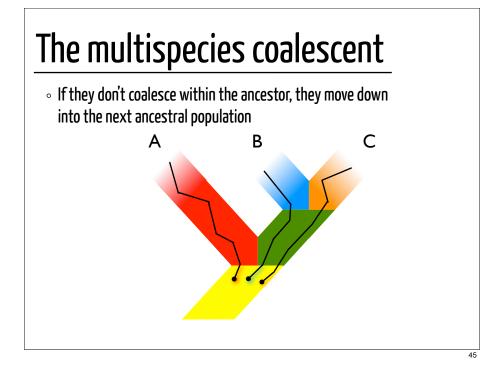
• Likewise, if we sample one allele from each of two <u>different</u> species, there is some probability that the two alleles will coalesce in the ancestor

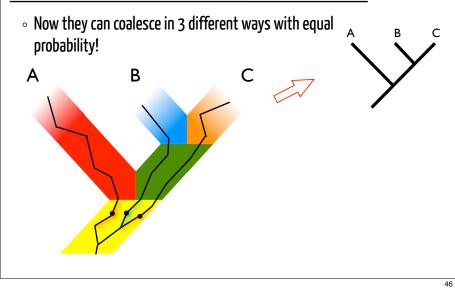


### The multispecies coalescent

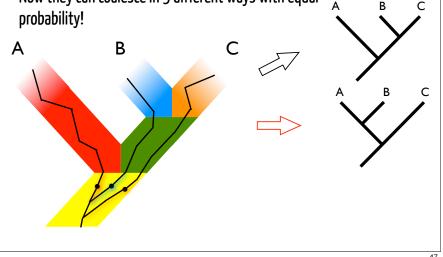
- But there is also some probability that they will not.
  - This is called incomplete coalescence
- What does the probability depend on?

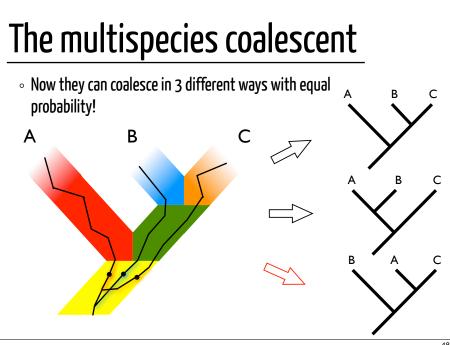






### The multispecies coalescent • Now they can coalesce in 3 different ways with equal





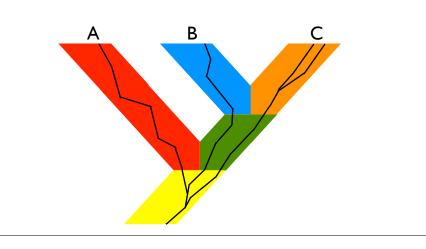
- $\,\circ\,$  Only 1 of the 3 matches the actual species phylogeny
  - So if there is an incomplete coalescence event in the alleles that we sampled, we have a 2/3rds chance of getting the wrong tree
- How do we determine the probability of incomplete coalescence?

### The multispecies coalescent

- The probability depends on the coalescent process that occurs within each lineage
  - We can break up the tree into its component parts
  - Each part has an 'input' and an 'output' number of lineages
    - $\,\circ\,$  Inherits the input from what happens above it
    - Output depends on the population size and the duration of the branch

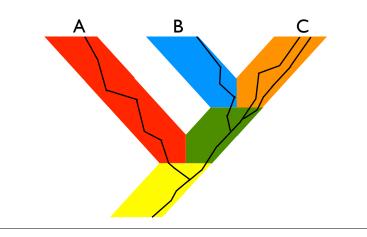
### The multispecies coalescent

• Gene 1 might look like this



### The multispecies coalescent

• While another gene looks like this. Each gene tree is an independent sample.



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• So does our phylogenetic sampling

• I.e., does our tree of individuals

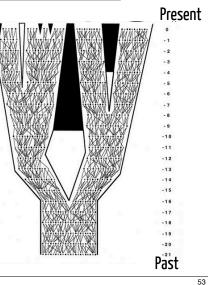
match our tree of species?

on the population sizes and

• Answer: Not necessarily, it depends

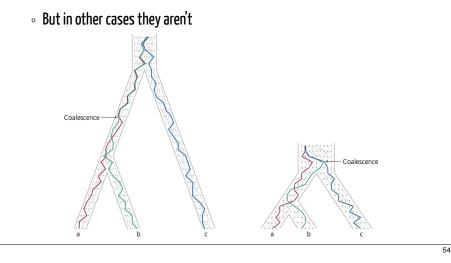
cause problems?

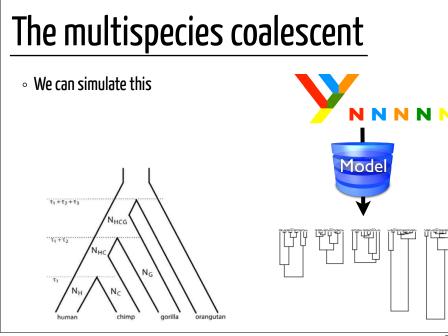
durations



### The multispecies coalescent

 $\circ~$  For some species, gene trees are fantastic estimates of the species tree





### **Empirical Example**

### OPEN 🗟 ACCESS Freely available online

### PLOS GENETICS

Widespread Discordance of Gene Trees with Species Tree in *Drosophila*: Evidence for Incomplete Lineage Sorting

Daniel A. Pollard<sup>1</sup>, Venky N. Iyer<sup>2®</sup>, Alan M. Moses<sup>1®</sup>, Michael B. Eisen<sup>1,2,3,4\*</sup>

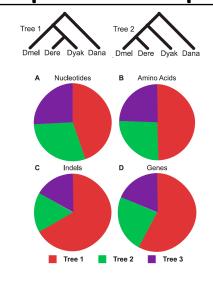
- Genomic data for each of:
  - 。 D. ananassae outgroup
  - D. melanogaster
  - D. erecta
  - D. yakuba

### **Empirical Example**





### **Empirical Example**



Nucleotide substitutions (in 9405 genes): Tree1-170,002, Tree 2-112,278, Tree 3- 98,117.

Gene trees (under ML): Tree 1- 5,381, Tree 2- 2,188, Tree 3-1,746

Conclude: Tree 1 ((erecta,yakuba), melano) wins, but lineage sorting is a huge problem.

Pollard et al. 2006

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### **Empirical Example**

• Human, Chimp, Gorilla

OPEN CACCESS Freely available online

Look at distribution of genome trees across the entire genome

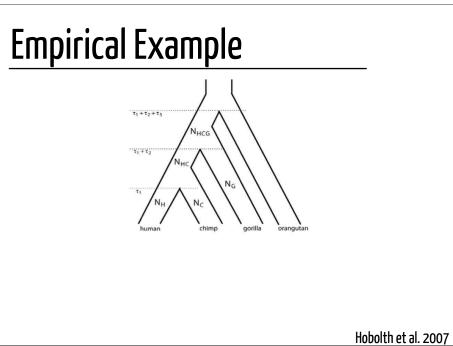
PLOS genetics

Pollard et al. 2006

Genomic Relationships and Speciation Times of Human, Chimpanzee, and Gorilla Inferred from a Coalescent Hidden Markov Model

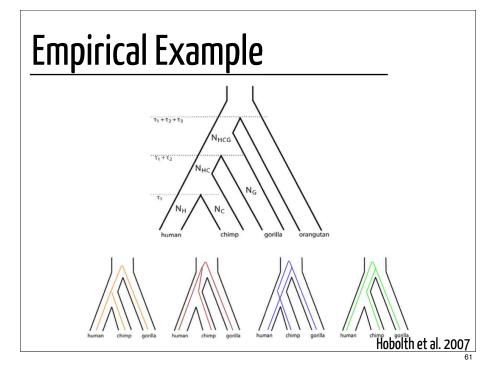
Asger Hobolth<sup>1\*</sup>, Ole F. Christensen<sup>2</sup>, Thomas Mailund<sup>2,3</sup>, Mikkel H. Schierup<sup>2</sup>

1 Bioinformatics Research Center, North Carolina State University, Raleigh, North Carolina, United States of America, 2 Bioinformatics Research Center, University of Aarhus, Aarhus, Denmark, 3 Department of Statistics, University of Oxford, Oxford, United Kingdom

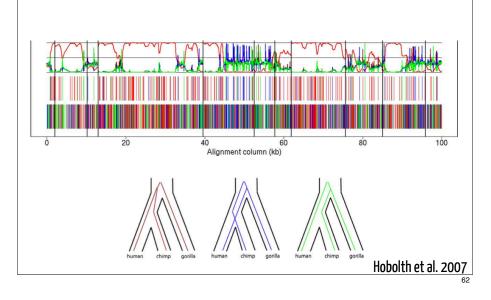


Tree 3

Dmel Dvak Dere

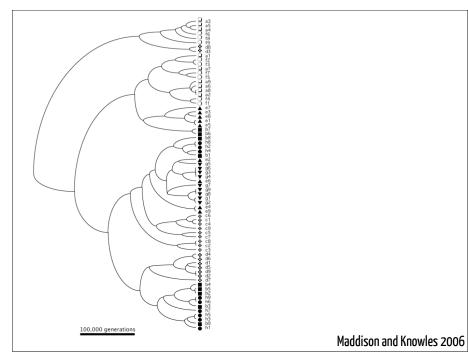


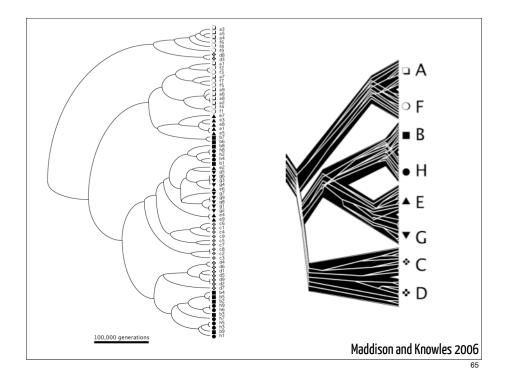
### **Empirical Example**



### Minimize Deep Coalescence

 given a set of gene trees, find the species tree that minimizes the implied number of deep coalescences (Maddison 1997, Maddison and Knowles 2006)





### Minimize Deep Coalescence

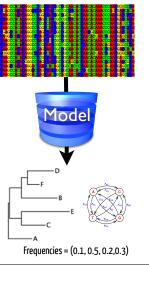
- $\circ~\mbox{simple}$  and intuitive
- but ignores important information (branch lengths), no measure of support
- software packages
  - $\circ$  mesquite
  - ∘ deep
  - $\circ$  Phylonet
- Doesn't explicitly model the coalescent process, places all probably on single histories

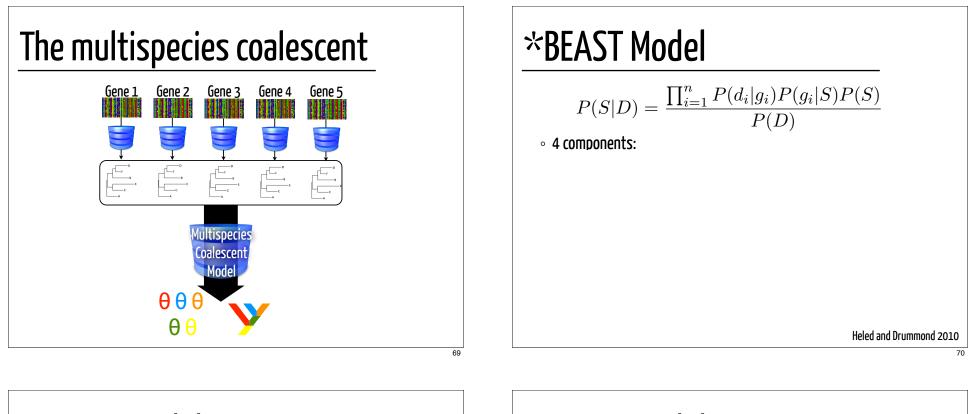
### Multispecies coalescent inference

- Perhaps a better solution:
  - We have this nice model, we can use statistical inference to infer species trees from gene trees and/or alignments

### Statistical inference

- What we've been doing:
- Inference under the MC, in the most general case, simply involves adding another level to this model.





### \*BEAST Model

$$P(S|D) = \frac{\prod_{i=1}^{n} P(d_i|g_i) P(g_i|S) P(S)}{P(D)}$$

• 4 components:

 $\circ P(d_i|g_i)$ - standard likelihood for alignment and gene tree i

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Heled and Drummond 2010

### \*BEAST Model

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• 4 components:

 $\circ P(d_i|g_i)$ - standard likelihood for alignment and gene tree i

 ${}_{\circ}P(g_i|S)\text{-}$  coalescent likelihood of gene trees

- $\circ \ P(S)$  uniform topology  $\qquad \qquad P(D)$  normalizing constant
  - birth-death or Yule branching
  - gamma pop sizes with hyperprior

Heled and Drummond 2010

### \*BEAST

### $P(g_i|S)$

- $\circ\,$  Likelihood of gene trees given the species tree
- We have an equation to calculate the likelihood of coalescent histories <u>within a lineage</u>

$$\mathbf{P}(L|N(t)) = \prod_{i=2}^{n} \frac{\binom{n}{2}}{N(t)} \exp\left(-\int_{0}^{t} \frac{\binom{n}{2}}{N(t)} dt\right)$$

 $\circ~$  How might we extend this to a whole tree?

Heled and Drummond 2010

 $\overset{*}{\underset{eq}{\text{SPEAST}}$ • Answer: Treat the likelihood of the coalescent history on each lineage independently  $= \prod_{i=2}^{n} \frac{\binom{n}{N}}{N(t)} \exp\left(-\int_{0}^{t} \frac{\binom{n}{N}}{N(t)} dt\right) \times \\ Helt and Drummod 210$ 

### **\*BEAST**

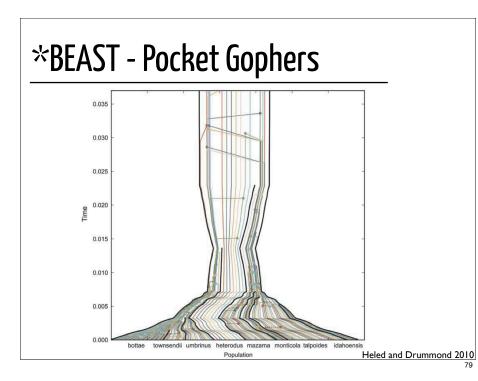
 $\circ$  Answer: Treat the likelihood of the coalescent history on each lineage independently  $\mathbf{P}(g|S) = \prod_{b \in S} \mathbf{P}(L_b(g)|N_b(t))$ 

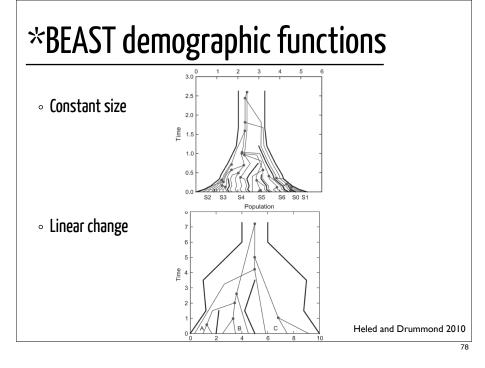
### \*BEAST

$$P(S|D) = \frac{\prod_{i=1}^{n} P(d_i|g_i) P(g_i|S) P(S)}{P(D)}$$

- Assumptions and limitations:
  - lineage sorting only source of incongruence
  - no gene flow following speciation
  - Implements a couple of demographic functions

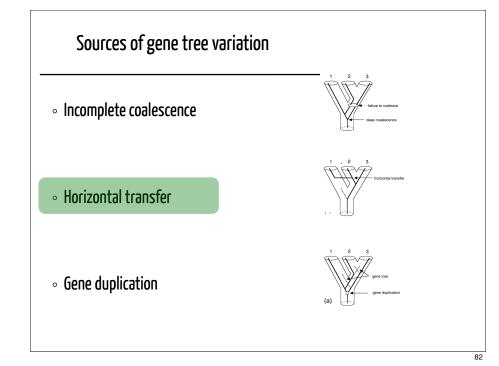
Heled and Drummond 2010

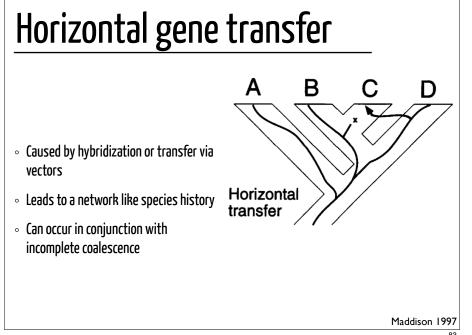






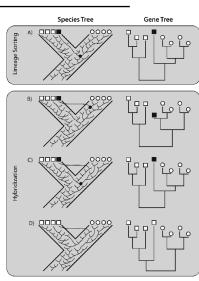






### Horizontal gene transfer

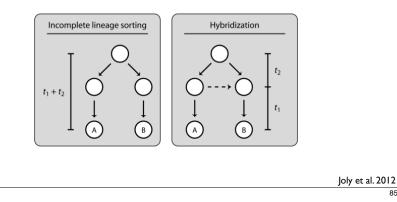
- Work on this is starting to emerge but is less well developed (so far)
- Basic idea is to use the distribution of branching times to detect shallow branching events that are unlikely under the coalescent



Joly et al. 2012

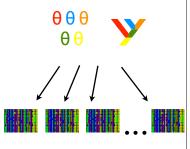
### Horizontal gene transfer

 One approach: uses a technique called posterior predictive simulation to assess the probability of observing "young" nodes under the multispecies coalescent by itself



### Horizontal gene transfer

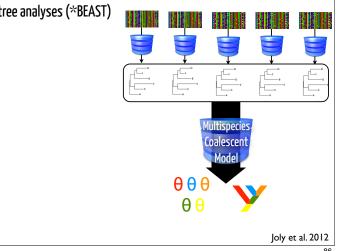
- Steps for posterior predictive simulation:
  - perform species tree analyses (\*BEAST)
  - Sample species trees, branch lengths, and population sizes from the posterior distribution



 $\,\circ\,$  Use these samples to simulate sequences

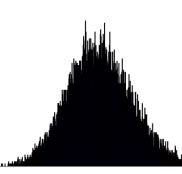
# Horizontal gene transfer

- Steps for posterior predictive simulation:
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### Horizontal gene transfer

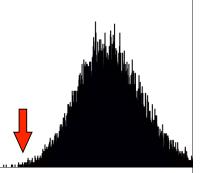
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  - Find the minimum pairwise distance between simulated sequences for your species of interest



Posterior predictive distribution of minimum pairwise divergences

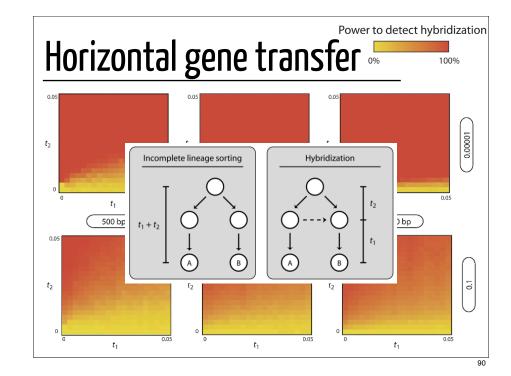
### Horizontal gene transfer

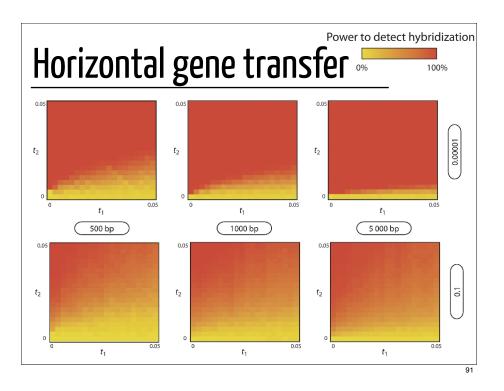
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  - Compare the minimum observed pairwise
     difference to construct p-value
     p = P(minDist(AB) < mindDist(AB)^{sim})</li>

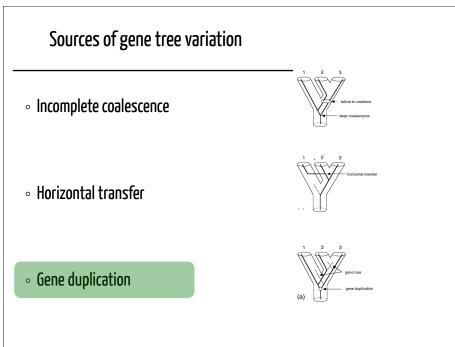


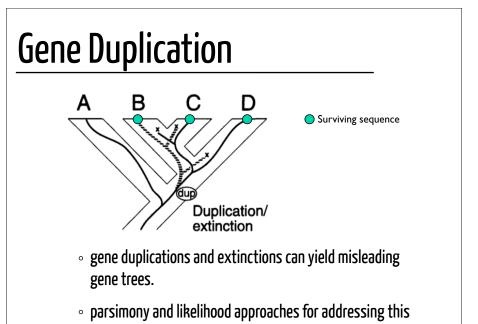
Posterior predictive distribution of minimum pairwise divergences

> Joly et al. 2012 89









Maddison 1997

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### **Gene Duplication**

- One solution: Just avoid the problem altogether
  - $\circ\,$  This may often be the best option
- For well characterized genomes, focus on known single copy genes

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  - Need to be careful about automated homology assignment

### **Gene Duplication**

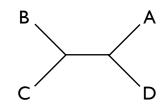
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  - $\circ\,$  This may often be the best option
- For well characterized genomes, focus on known single copy genes
- $\circ~$  More problematic with large genome scale datasets
  - Need to be careful about automated homology assignment
- $\circ~$  There are some methods to accommodate this

## Gene Tree Parsimony

- input a collection of rooted gene trees, find the species tree that minimizes the reconciliation cost
  - reconciliation cost is number of duplications, or duplications and losses, summed across gene trees

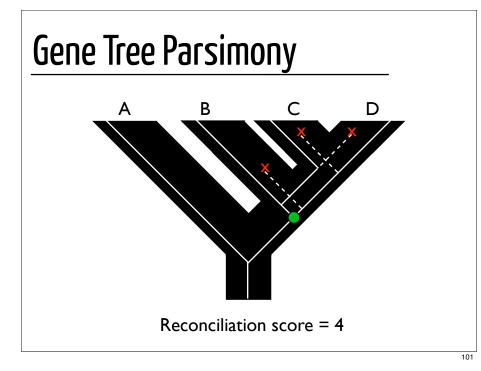
## Gene Tree Parsimony

 $\circ~$  example gene tree:



• calculate reconciliation costs for species trees

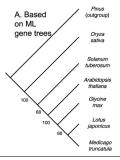
# Gene Tree Parsinony A B C D V C D D V C D D Reconciliation score = 5 C C D

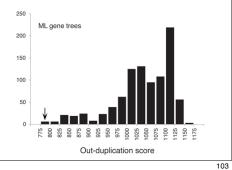


# Gene Tree Parsimony

### **Empirical Example**

- Sanderson and McMahon 2007
  - GTP analysis of 576 gene trees for 6 angiosperm species (plus outgroup)
  - known species tree recovered successfully despite massive gene duplication



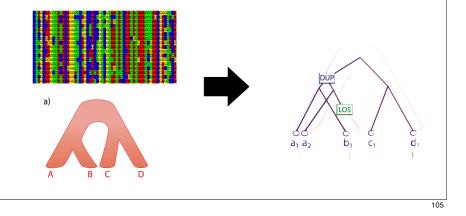


### Gene Tree Parsimony

- small trees Gtp (Sanderson and McMahon 2007)
- large trees DupTree (Wehe et al 2008)

### **Statistical Approaches**

• Likelihood methods for inferring gene trees and duplication and loss history <u>given</u> a species tree have existed for some time



### Statistical Approaches

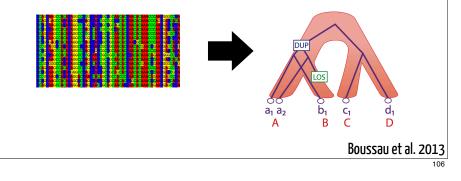
- Likelihood methods for inferring gene trees and duplication and loss history <u>given</u> a species tree have existed for some time
- $\circ~$  Until recently, no methods available to do the joint inference

$$\underbrace{L(T, S, N|A)}_{i \in \mathcal{G}} = \prod_{i \in \mathcal{G}} L(S, N|T_i) L(T_i|A_i)$$

Boussau et al. 2013

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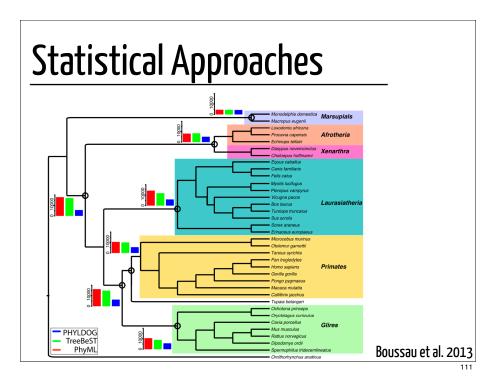
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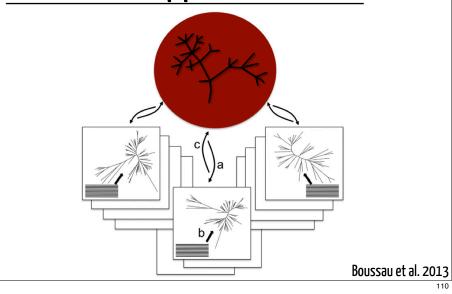
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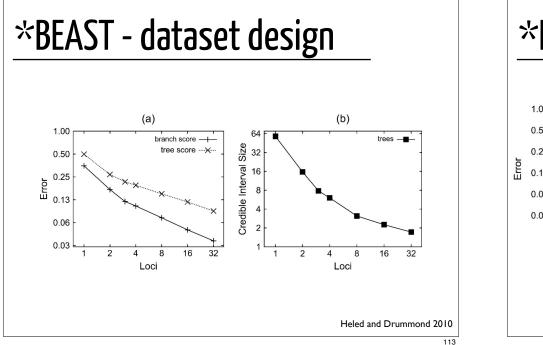
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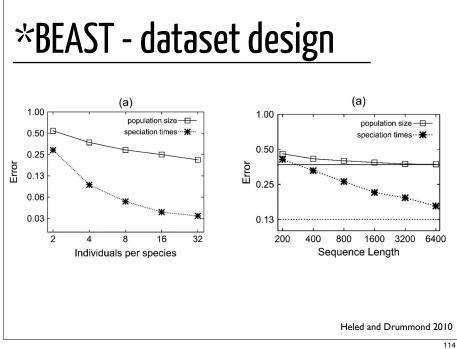


### Wrapping up

### • Some thoughts:

- There are several options here, you should carefully choose a model based on biological knowledge
- $\circ\,$  Need for more simulation studies
  - $\circ~$  Sensitivities to priors and demographic functions
- Data needs are substantial





### Difficulties

- Often making some strong assumptions about changes or constancy of population sizes
  - Not always well known how robust it is to deviations from the correct model
- Power attenuates throughout the tree
- Mixing problems are common